

Introduction to Information Retrieval

<http://informationretrieval.org>

IIR 12: Language Models for IR

Hinrich Schütze

Institute for Natural Language Processing, Universität Stuttgart

2011-08-29

Models and Methods

- 1 Boolean model and its limitations (30)
- 2 Vector space model (30)
- 3 Probabilistic models (30)
- 4 **Language model-based retrieval (30)**
- 5 Latent semantic indexing (30)
- 6 Learning to rank (30)

Take-away

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- Statistical language models: Introduction

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- Statistical language models in IR

Take-away

- Statistical language models: Introduction
- Statistical language models in IR
- Discussion: Properties of different probabilistic models in use in IR

Outline

- 1 Statistical language models
- 2 Statistical language models in IR
- 3 Discussion

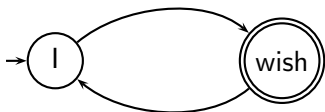
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We can view a **finite state automaton** as a **deterministic** language model.

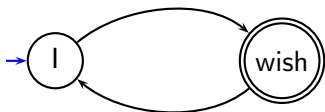
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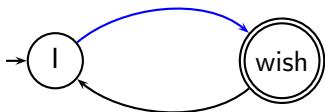
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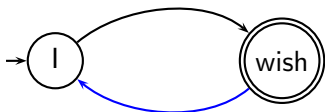
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I wish

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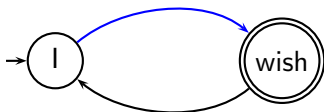
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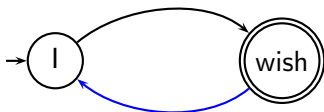
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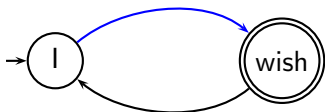
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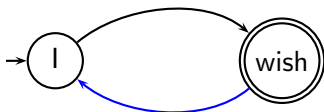
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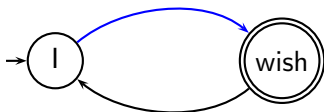
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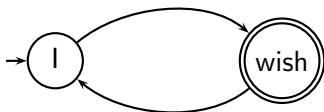
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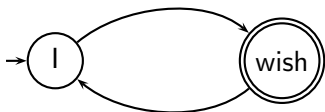
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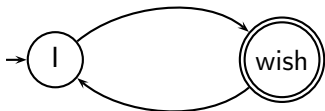


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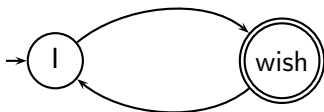
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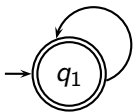
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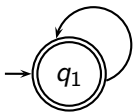
A probabilistic language model



w	$P(w q_1)$	w	$P(w q_1)$
STOP	0.2	toad	0.01
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This is a one-state probabilistic finite-state automaton – a **unigram language model** – and the state emission distribution for its one state q_1 .

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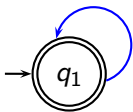


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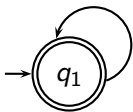
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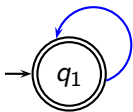
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$$P(\text{string}) = 0.01$$

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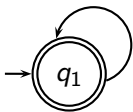
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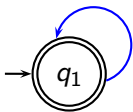
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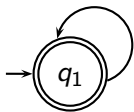
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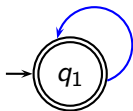
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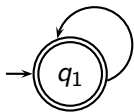
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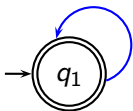
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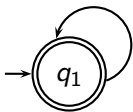
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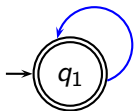
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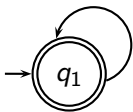
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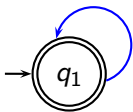
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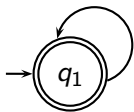
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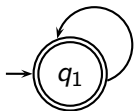
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$$\begin{aligned}
 P(\text{string}) &= 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2 \\
 &= 0.00000000000048
 \end{aligned}$$



A different language model for each document

language model of d_1

w	$P(w .)$	w	$P(w .)$
STOP	.2	toad	.01
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a	.1	likes	.02
frog	.01	that	.04
	

language model of d_2

w	$P(w .)$	w	$P(w .)$
STOP	.2	toad	.02
the	.15	said	.03
a	.08	likes	.02
frog	.01	that	.05
	

query: frog said that toad likes frog STOP

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language model of d_2

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query: frog said that toad likes frog STOP

$$\begin{aligned}
 P(\text{query}|M_{d_1}) &= 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2 \\
 &= 0.00000000000048 = 4.8 \cdot 10^{-12}
 \end{aligned}$$

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language model of d_2

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query: frog said that toad likes frog STOP

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$$= 0.00000000000048 = 4.8 \cdot 10^{-12}$$

$$P(\text{query}|M_{d_2}) = 0.01 \cdot 0.03 \cdot 0.05 \cdot 0.02 \cdot 0.02 \cdot 0.01 \cdot 0.2$$

$$= 0.00000000000120 = 12 \cdot 10^{-12}$$

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query: frog said that toad likes frog STOP

$$P(\text{query}|M_{d_1}) = 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2$$

$$= 0.0000000000048 = 4.8 \cdot 10^{-12}$$

$$P(\text{query}|M_{d_2}) = 0.01 \cdot 0.03 \cdot 0.05 \cdot 0.02 \cdot 0.02 \cdot 0.01 \cdot 0.2$$

$$= 0.0000000000120 = 12 \cdot 10^{-12}$$

$P(\text{query}|M_{d_1}) < P(\text{query}|M_{d_2})$ Thus, document d_2 is “more relevant” to the query “frog said that toad likes frog STOP” than d_1 is. □

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$$P(d|q) = \frac{P(q|d)P(d)}{P(q)}$$

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- $P(d)$ is the prior – often treated as the same for all d
 - But we can give a higher prior to “high-quality” documents, e.g., those with high PageRank.
- $P(q|d)$ is the probability of q given d .

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$$P(d|q) = \frac{P(q|d)P(d)}{P(q)}$$

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- $P(d)$ is the prior – often treated as the same for all d
 - But we can give a higher prior to “high-quality” documents, e.g., those with high PageRank.
- $P(q|d)$ is the probability of q given d .
- Under the assumptions we made, ranking documents according to $P(q|d)P(d)$ and $P(d|q)$ is equivalent. □

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- We need to smooth the estimates to avoid zeros. □

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- We will use $\hat{P}(t|M_C)$ to “smooth” $P(t|d)$ away from zero. \square

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- Tuning λ is important for good performance. □

Jelinek-Mercer smoothing: Summary



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- What we model: The user has a document in mind and generates the query from this document.
- $P(q|d)$ is the probability that the document that the user had in mind was in fact this one. □

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- Ranking: $d_2 > d_1$



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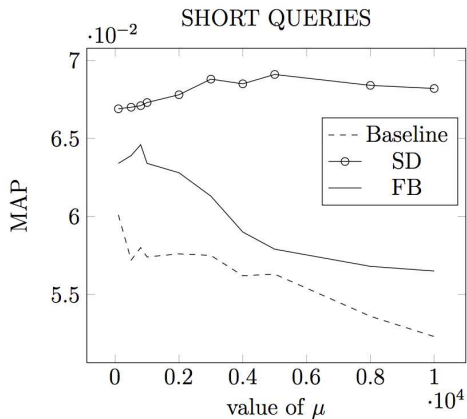
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- The weighting factor α determines how strong an effect the prior has. □

Jelinek-Mercer or Dirichlet?

- Dirichlet performs better for keyword queries, Jelinek-Mercer performs better for verbose queries.
- Both models are sensitive to the smoothing parameters – you shouldn't use these models without parameter tuning.

Sensitivity of Dirichlet to smoothing parameter



μ is the Dirichlet smoothing parameter (called α on the previous slides)



Vector space (tf-idf) vs. LM

Rec.	precision		%chg	significant
	tf-idf	LM		
0.0	0.7439	0.7590	+2.0	
0.1	0.4521	0.4910	+8.6	
0.2	0.3514	0.4045	+15.1	*
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... but note that where the approach shows significant gains is at higher levels of recall. □

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- 6 Present most likely document(s) to user



Outline

- 1 Statistical language models
- 2 Statistical language models in IR
- 3 Discussion

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generative model

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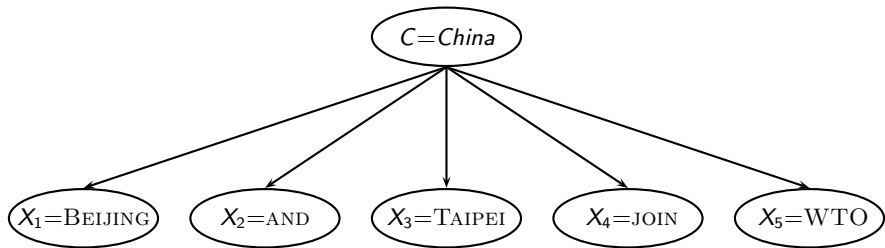
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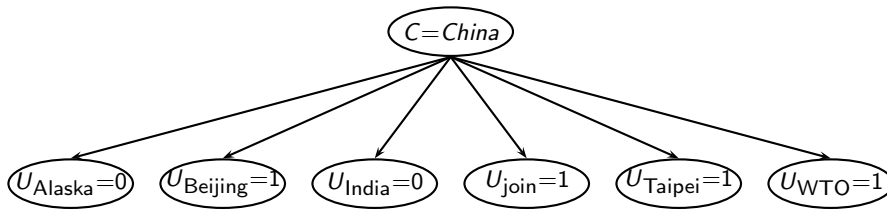
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Naive Bayes Multinomial model / IR language models



Naive Bayes Bernoulli model / Binary independence model



Comparison of the two models

	multinomial model / IR LM	Bernoulli model / BIM
event model	generation of (multi)set of tokens	generation of subset of vocabulary
random variable(s)	$X = t$ iff t occurs at given pos	$U_t = 1$ iff t occurs in doc
doc. representation	$d = \langle t_1, \dots, t_k, \dots, t_{n_d} \rangle, t_k \in V$	$d = \langle e_1, \dots, e_i, \dots, e_M \rangle,$ $e_i \in \{0, 1\}$
parameter estimation	$\hat{P}(X = t c)$	$\hat{P}(U_i = e c)$
dec. rule: maximize	$\hat{P}(c) \prod_{1 \leq k \leq n_d} \hat{P}(X = t_k c)$	$\hat{P}(c) \prod_{t_i \in V} \hat{P}(U_i = e_i c)$
multiple occurrences	taken into account	ignored
length of docs	can handle longer docs	works best for short docs
# features	can handle more	works best with fewer
estimate for THE	$\hat{P}(X = \text{the} c) \approx 0.05$	$\hat{P}(U_{\text{the}} = 1 c) \approx 1.0$

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- Collection frequency (LMs) vs. document frequency (BM25, vector space)



Take-away

- **Statistical language models:** Introduction
- **Statistical language models in IR**
- **Discussion:** Properties of different probabilistic models in use in IR

Resources

- Chapter 12 of Introduction to Information Retrieval
- Resources at <http://informationretrieval.org/essir2011>
 - Ponte and Croft's 1998 SIGIR paper (one of the first on LMs in IR)
 - Zhai and Lafferty: A study of smoothing methods for language models applied to information retrieval. ACM Trans. Inf. Syst. (2004).
 - Lemur toolkit (good support for LMs in IR)
 - Bernoulli vs multinomial models

Exercise: Compute ranking

- Collection: d_1 and d_2
- d_1 : Xerox reports a profit but revenue is down
- d_2 : Lucene narrows quarter loss but revenue decreases further
- Query q : revenue down
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- $P(q|d_1) = [(1/8 + 2/16)/2] \cdot [(1/8 + 1/16)/2] = 1/8 \cdot 3/32 = 3/256$
- $P(q|d_2) = [(1/8 + 2/16)/2] \cdot [(0/8 + 1/16)/2] = 1/8 \cdot 1/32 = 1/256$
- Ranking: $d_1 > d_2$